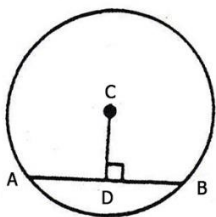


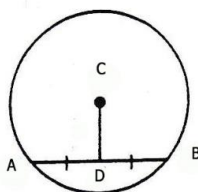
**Circle geometry:**

Secant line and Chord properties of a circle with the center C:

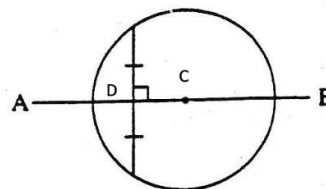
A perpendicular line from C bisects the chord:  $AD = DB$



A radius bisecting a chord at D is perpendicular to it:  $\angle CDA = 90^\circ$

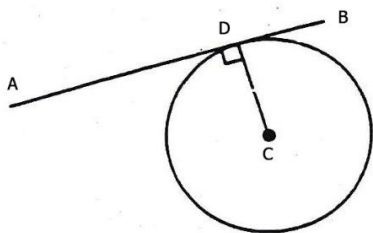


A line perpendicular bisector to any chord passes through C

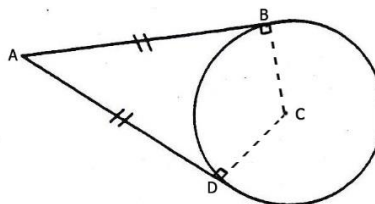


Tangent line Properties:

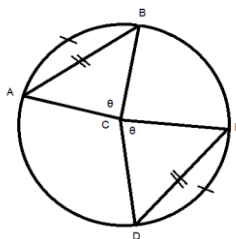
The radius CD, and the tangent line AB at the tangent point D, are perpendicular



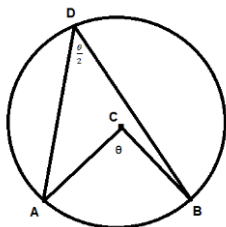
Two tangent line segments from an external point A to a circle, are equal:  $AB = AD$



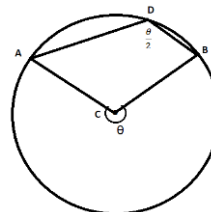
Central angles: Central angles subtended to equal arcs or chords are equal and vice versa



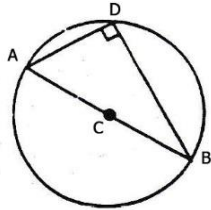
Inscribed angles: Inscribed angles are equal to the  $\frac{1}{2}$  central angles subtended to the same arc/chord



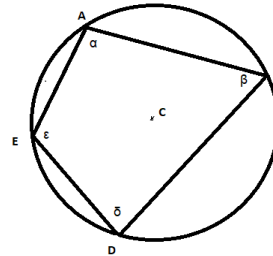
$$\angle ADB = \frac{1}{2} \angle ACB$$



Inscribed angles subtended to the diameter of a circle are always  $90^\circ$ . Half of central angle

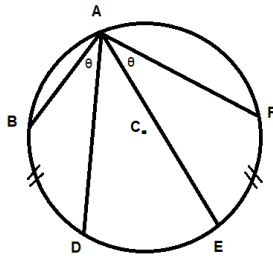


In a cyclic quadrilateral (inscribed in a circle) the sum of 2 opposite angles is  $180^\circ$ . Each one is half of its corresponding central angle

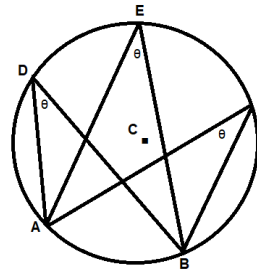


$$\alpha + \delta = 180^\circ \quad \text{and} \quad \beta + \epsilon = 180^\circ$$

Inscribed angles subtended to equal arc/chord are equal



Inscribed angles subtended to the same arc/chord AB, are equal



Inscribed angle and the tangent line to a circle:

A tangent line at the point A and the secant line AB, make an inscribed angle  $\theta$ , subtend to the chord AB, therefore any other inscribed angles subtended to the same chord AB, have the same angle  $\theta$

